

Eléments propres de

1. $A_1 = \begin{pmatrix} 7 & 2 & -2 \\ 2 & 4 & -1 \\ -2 & -1 & 4 \end{pmatrix}$. *Rép* : $X_{A_1}(X) = (X - 3)^2(X - 9)$, $E_3(A_1) = \text{Vect}((1, -2, 0), (0, 1, 1))$, $E_9(A_1) = \text{Vect}((2, 1, -1))$.
2. $A_2 = \begin{pmatrix} 9 & 1 & 6 \\ -7 & 1 & -6 \\ -10 & -1 & -7 \end{pmatrix}$. *Rép* : $X_{A_2}(X) = (X - 2)^2(X + 1)$, $E_{-1}(A_2) = \text{Vect}((-2, 2, 3))$, $E_2(A_2) = \text{Vect}((-1, 1, 1))$.
3. $A_3 = \begin{pmatrix} -2 & -1 & 2 \\ -15 & -6 & 11 \\ -14 & -6 & 11 \end{pmatrix}$. *Rép* : $X_{A_3}(X) = (X - 1)^3$, $E_1(A_3) = \text{Vect}((1, 1, 2))$.
4. $A_4 = \begin{pmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 3 \end{pmatrix}$. *Rép* : $X_{A_4}(X) = (X - 1)(X - 3)^2$, $E_3(A_4) = \text{Vect}((1, 1, 0))$, $E_1(A_4) = \text{Vect}((-1, 1, 0))$.
5. $A_5 = \begin{pmatrix} -1 & 0 & 3 \\ -3 & 2 & 3 \\ 0 & 0 & 2 \end{pmatrix}$. *Rép* : $X_{A_5}(X) = (X + 1)(X - 2)^2$, $E_2(A_5) = \text{Vect}((1, 0, 1), (0, 1, 0))$, $E_{-1}(A_5) = \text{Vect}((1, 1, 0))$.
6. $A_6 = \begin{pmatrix} 0 & 0 & 4 \\ 1 & 0 & -8 \\ 0 & 1 & 5 \end{pmatrix}$. *Rép* : $X_{A_6}(X) = (X - 1)(X - 2)^2$, $E_2(A_6) = \text{Vect}((2, -3, 1))$, $E_1(A_6) = \text{Vect}((4, -4, 1))$.
7. $A_7 = \begin{pmatrix} 2 & 1 & 1 \\ 0 & 0 & -2 \\ 0 & 1 & 3 \end{pmatrix}$. *Rép* : $X_{A_7}(X) = (X - 1)(X - 2)^2$, $E_2(A_7) = \text{Vect}((1, 0, 0), (0, 1, -1))$, $E_1(A_7) = \text{Vect}((-2, 1, 1))$.
8. $A_8 = \begin{pmatrix} -2 & 1 & 1 \\ 8 & 1 & -5 \\ 4 & 3 & -3 \end{pmatrix}$. *Rép* : $X_{A_8}(X) = X(X + 2)^2$, $E_2(A_8) = \text{Vect}((1, -1, 1))$, $E_0(A_8) = \text{Vect}((3, 1, 5))$.
9. $A_9 = \begin{pmatrix} 16 & 1 & 1 & 1 \\ 1 & 16 & 1 & 1 \\ 1 & 1 & 16 & 1 \\ 1 & 1 & 1 & 16 \end{pmatrix}$. *Rép* : $X_{A_9}(X) = (X - 15)^3(X - 19)$, $E_{15}(A_9) = \text{Vect}((1, -1, 0, 0), (1, 0, -1, 0), (1, 0, 0, -1))$,
 $E_{19}(A_9) = \text{Vect}((1, 1, 1, 1))$.
10. $A_{10} = \begin{pmatrix} 1 & a & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$.