

$$\underline{1.} \quad U_m(p) + E_m(p) = (R + Lp)I_m(p) \quad (2)$$

$$E_m(p) = K_e \Omega_m(p)$$

$$J_m \times p \times \Omega_m(p) = C_m(p)$$

$$C_m(p) = K_c I_m(p)$$

2.



$$\underline{3.} \quad H(p) = \frac{K_c}{Jp(R+Lp)} = \frac{K_c}{K_c K_e + Jp(R+Lp)}$$

$$= \frac{1}{K_e} \frac{1}{1 + \frac{JR}{K_c K_e} p + \frac{JL}{K_c K_e} p^2}$$

4.

$$K = 1/K_e$$

$$\frac{1}{\omega_0^2} = \frac{JL}{K_c K_e} \Rightarrow \omega_0 = \sqrt{\frac{K_c K_e}{JL}}$$

$$\frac{2\zeta}{\omega_0} = \frac{JR}{K_c K_e} \Rightarrow \zeta = 2 \frac{JR}{K_c K_e} \times \sqrt{\frac{K_c K_e}{JL}} = 2 \sqrt{\frac{J}{K_c K_e}} \times L$$

5.

$$H(p) = \frac{K}{(1+\tau_e p)(1+\tau_m p)} = \frac{K}{1 + (\tau_e + \tau_m)p + \tau_e \tau_m p^2}$$

$$(\tau_e + \tau_m) = \frac{JR}{K_c K_e}$$

$$\tau_e \tau_m = \frac{JL}{K_c K_e}$$

6.

$$\tau_e \ll \tau_m \Rightarrow \tau_e + \tau_m \approx \tau_m \Rightarrow H = \frac{K}{1 + \tau_m p}$$

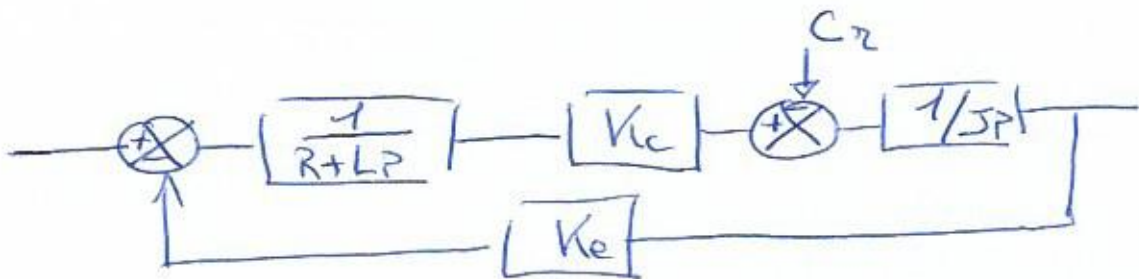
$$\tau_e \tau_m \approx 0$$

②

$$\begin{aligned}
 \underline{7.} \quad \omega_m(+\infty) &= \lim_{t \rightarrow \infty} \omega_m(t) \\
 &= \lim_{p \rightarrow \infty} p \Omega_m(p) \\
 &= \lim_{p \rightarrow \infty} p H(p) \cdot E(p) \\
 &= \lim_{p \rightarrow \infty} \frac{18 \times p \times H(p)}{p} = \lim_{p \rightarrow \infty} 18 \times H(p) \\
 &= 18 \times K
 \end{aligned}$$

$$\begin{aligned}
 \underline{8.} \quad \omega_m(+\infty) &= 18 \times K = 18 \times 45 \text{ rad} \cdot \text{s}^{-1} \\
 &= \frac{18 \times 45}{60 \times 2\pi}
 \end{aligned}$$

9.



$$\underline{10.} \quad F_1(p) = \frac{K}{1 + \zeta_m p}$$

$$F_2(p) = \frac{1/Js}{1 + \frac{KcKe}{Js(R+Lp)}}$$

11 On veut $F(p) \times \Omega(p)$.

$$B(p)\Omega(p) - C_2(p) = \frac{\Omega_m}{F(p)}$$

D'après 10: $\Omega_m(p) = F_1(p)\Omega(p) + F_2(p)C_2(p)$

$$\frac{\Omega_m(p)}{F_2(p)} = \frac{F_1(p)}{F_2(p)} \Omega(p) - C_2(p)$$

$$B(p) = \frac{F_1(p)}{F_2(p)} \quad \text{et} \quad F(p) = \frac{1}{F_2(p)}$$

12. $M(p) = \frac{1}{p}$ car $\Theta_a = \int \omega_a(t) dt$ (3)

$G(p) = \frac{1}{N}$ car $\frac{\omega_a}{\omega_m} = \frac{1}{N}$

13 $H_a(p) = \frac{K_a \times \frac{K}{1 + \zeta_m p} * \frac{1}{N} \times \frac{1}{p}}$

$$= \frac{1 + \frac{K_a K}{N p (1 + \zeta_m p)}}{K_a K + N p (1 + \zeta_m p)}$$

14 $E = \sum_{t \rightarrow \infty} (e(t) - s(t)) = \sum_{p \rightarrow \infty} p (E(p) - S(p))$

$$= \sum_{p \rightarrow \infty} \frac{\bar{E}_0}{p} p (1 - H(p))$$

$$= \sum_{p \rightarrow \infty} \bar{E}_0 \left(1 - \frac{K_a K}{K_a K + N p (1 + \zeta_m p)} \right)$$

$$= \bar{E}_0 \left(1 - \frac{K_a K}{K_a K} \right) = 0$$